Class $\mathbf{- 1 2}^{\text {th }}$
Worksheet-12

Chapter-4

1. Show that $\left|\begin{array}{ccc}a & b & c \\ a+2 x & b+2 y & c+2 z \\ x & y & z\end{array}\right|=0$
2. Prove that $\left|\begin{array}{ccc}a & a+b & a+b+c \\ 2 a & 3 a+2 b & 4 a+3 b+2 c \\ 3 a & 6 a+3 b & 10 a+6 b+3 c\end{array}\right|=a^{3}$
3. If $x, y, z$ are different and $\Delta=\left|\begin{array}{ccc}x & x^{2} & 1+x^{3} \\ y & y^{2} & 1+y^{3} \\ z y z=0 & z^{2} & 1+z^{3}\end{array}\right|=0$, then show that $1+$
4. Show that

$$
\left|\begin{array}{ccc}
1+a & 1 & 1 \\
1 & 1+b & 1 \\
1 & 1 & 1+c
\end{array}\right|=a b c\left(1+\frac{1}{a}+\frac{1}{b}+\frac{1}{c}\right)=a b c+b c+c a+a b
$$

Using the property of determinants and without expanding, prove that:
5. $\left|\begin{array}{lll}1 & b c & a(b+c) \\ 1 & c a & b(c+a) \\ 1 & a b & c(a+b)\end{array}\right|=0$
6. $\left|\begin{array}{ccc}-a^{2} & a b & a c \\ b a & -b^{2} & b c \\ c a & c b & -c^{2}\end{array}\right|=4 a^{2} b^{2} c^{2}$

