

Class – 12<sup>th</sup>

Chapter-5

Subject Maths

Worksheet-24

Inverse of a Matrix and Linear Equations

1. Solve the equations using matrix method:

(i)  $2x - y = -2$

(ii)  $5x + 7y + 2 = 0$

$3x + 4y = 3$

$4x + 6y + 3 = 0$

2. If  $A = \begin{bmatrix} 1 & -2 & 0 \\ 2 & 1 & 3 \\ 0 & -2 & 1 \end{bmatrix}$  then find  $A^{-1}$  and solve the system of equations:

$x - 2y = 10, \quad 2x + y + 3z = 8, \quad -2y + z = 7.$

3. Find the product of matrices  $\begin{bmatrix} -4 & 4 & 4 \\ -7 & 1 & 3 \\ 5 & -3 & -1 \end{bmatrix}$  and  $\begin{bmatrix} 1 & -1 & 1 \\ 1 & -2 & 2 \\ 2 & 1 & 3 \end{bmatrix}$  and solve

the system of equations using the above product

$x - y + z = 4$

$x - 2y - 2z = 9$

$2x + y + 3z = 1$

4. Find the inverse of the matrix  $\begin{bmatrix} 1 & -1 & 1 \\ 2 & 1 & -3 \\ 1 & 1 & 1 \end{bmatrix}$  and with the help of this solve the

system of equations  $\begin{bmatrix} 1 & 0 & 1 \\ 2 & 1 & 0 \\ 0 & 1 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \frac{1}{2} \begin{bmatrix} 2y \\ 6z \\ -2x \end{bmatrix} + 2 \begin{bmatrix} 2 \\ 0 \\ 1 \end{bmatrix}$

5. If the side of an equilateral triangle is  $a$  and vertices are

$(x_1, y_1), (x_2, y_2)$  and  $(x_3, y_3)$  then prove that

$$\begin{vmatrix} x_1 & y_1 & 2 \\ x_2 & y_2 & 2 \\ x_3 & y_3 & 2 \end{vmatrix}^2 = 3a^4$$