

Class – 12<sup>th</sup>

Chapter-7

Subject Maths

Worksheet-32

Differentiation

1. Verify Rolle's theorem for the functions given below:

(a)  $f(x) = e^x(\sin x - \cos x)$ ;  $x \in [\pi/4, 5\pi/4]$  (b)  $f(x) = (x-a)^m(x-b)^n$ ;  $x \in [a, b], m, n \in N$

(c)  $f(x) = |x|$ ;  $x \in [-1, 1]$

(d)  $f(x) = x^2 + 2x - 8$ ;  $x \in [-4, 2]$

(e)  $f(x) = \begin{cases} x^2 + 1 & ; 0 \leq x \leq 1 \\ 3 - x & ; 1 < x \leq 2 \end{cases}$

(f)  $f(x) = [x]$ ;  $x \in [-2, 2]$

2. Verify Rolle's theorem for the functions given below :

(a)  $f(x) = x^2 + 5x + 6$ ;  $x \in [-3, -2]$

(b)  $f(x) = e^{-x} \sin x$ ;  $x \in [0, \pi]$

(c)  $f(x) = \sqrt{x(1-x)}$ ;  $x \in [0, 1]$

(d)  $f(x) = \cos 2x$ ;  $x \in [0, \pi]$

3. Verify Lagrange's mean value theorem for the functions given below:

(a)  $f(x) = x + \frac{1}{x}$ ;  $x \in [1, 3]$

(b)  $f(x) = \frac{x^2 - 4}{x - 1}$ ;  $x \in [0, 2]$

(c)  $f(x) = x^2 - 3x + 2$ ;  $x \in [-2, 3]$

(d)  $f(x) = \frac{1}{4x - 1}$ ;  $x \in [1, 4]$