

Class – 12<sup>th</sup>

Chapter-8

Subject Maths

Worksheet-34

Application of Derivatives

1. Find the rate of change of the area of a circle with respect to radius  $r$ , when  $r = 3$  cm and  $r = 4$  cm.
2. A particle is moving along the curve  $y = \frac{2}{3}x^3 + 1$ . Find the points on the curve at which the  $y$ -coordinate is changing twice as fast as the  $x$  coordinate.
3. A ladder 13 m long is leaning against a wall. The bottom of the ladder is pulled along the ground, from the wall, at the rate of 1.5 m/s. How fast is its height on the wall decreasing when the foot of the ladder is 12 m away from the wall?
4. An edge of a variable cube is increasing at the rate of 3 cm/s. Find the rate at which the volume of the cube is increasing when the edge is 10 cm long?
5. A balloon which always remains spherical on inflation, is being inflated by pumping at the rate of 900 cm<sup>3</sup>/s. of gas. Find the rate at which the radius of balloon increases when the radius is 15 cm.
6. A balloon, which always remains spherical has a variable diameter  $\frac{3}{2}(2x+1)$ . Find the rate at which its volume is increasing with respect to  $x$ .
7. The total cost  $C(x)$  rupees, associated with the production of  $x$  units of an item is given by
$$C(x) = 0.005x^3 - 0.02x^2 + 30x + 5000$$
Find the marginal cost when 3 units are produced, here by marginal cost we mean the instantaneous rate of change of total cost at any level of output.
8. The radius of a soap bubble is increasing at the rate of 0.2 cm/s. Find the rate of increase in surface area when the radius is 7 cm. Also find the rate of change in volume when the radius is 5 cm.